

Table 1. The validated state transitions from a State $S_i(k)$ to State $S_j(k+1)$

	$S_h(k+1)$	$S_c(k+1)$	$S_s(k+1)$	$S_u(k+1)$	$S_p(k+1)$	$S_d(k+1)$	$S_e(k+1)$
$S_h(k)$	$R_{h,h}$	$R_{h,c}$	0	0	0	0	0
$S_c(k)$	$R_{c,h}$	$R_{c,c}$	$R_{c,s}$	0	0	0	0
$S_s(k)$	0	$R_{s,c}$	0	$R_{s,u}$	0	0	0
$S_u(k)$	0	0	$R_{u,s}$	$R_{u,u}$	$R_{u,p}$	0	0
$S_p(k)$	0	0	0	0	0	$R_{p,d}$	0
$S_d(k)$	0	0	0	$R_{d,u}$	0	$R_{d,d}$	$R_{d,e}$
$S_e(k)$	$R_{e,h}$	0	0	0	0	0	0

Equation (1), (2) and (3):

If,

- l denotes the year
- L is the current year
- m is the number of years with historical data available
- i denotes the day of the month
- j is the month of a year. (an exemplary time unit used for simplified demonstration purposes only)

Thus, $i \in [1, 31]$, $j \in [1, 12]$, l and m are integers.

$$\bar{x}_j = \frac{1}{m \times n} \sum_{l=L-m}^{L-1} \sum_{i=1}^n x_{l,j,i} \quad (\text{where } i \in [1, 31] \text{ and } j \in [1, 12]) \quad (1)$$

$$s_j = \frac{1}{(m \times n - 1)} \sqrt{\sum_{l=L-m}^{L-1} \sum_{i=1}^n (x_{l,j,i} - \bar{x}_j)^2} \quad (\text{where } i \in [1, 31] \text{ and } j \in [1, 12]) \quad (2)$$

$$C_j = \bar{x}_j + t_{m \times n - 1} s_j \quad (\text{where } i \in [1, 31] \text{ and } j \in [1, 12]) \quad (3)$$

Equation (4), (5) and (6):

$$d_{L,j,i} = \frac{x_{L,j,i} - \bar{x}_j}{\bar{x}_j} \times 100 \quad (L - \text{year}, j - \text{month}, i - \text{day of month}) \quad (4)$$

$$w_{L,j,i} = \sum_{n=0}^{n=6} d_{L,j,i-n} \quad (7 - \text{days cumulated deviation}) \quad (5)$$

$$v_{L,j,i} = d_{L,j,i} - d_{L,j,i-1} \quad (\text{change of the daily deviation}) \quad (6)$$

Equation (7), (8) and (9):

$$\text{supp}(\alpha(k)) = \{d_{l < L, j, i}; F(d) \geq (1 - \alpha)\} \quad (7)$$

$$\text{supp}(\beta(k)) = \{w_{l < L, j, i}; F(w) \geq (1 - \beta)\} \quad (8)$$

$$\text{supp}(\delta(k)) = \{v_{l < L, j, i}; F(v) \geq (1 - \delta)\} \quad (9)$$

Equation (10), (11), (12), (13), (14) and (15):

$$S_j(k+1) \Leftarrow \{S_i(k) \otimes R_{i,j} \otimes X_i(k), S_i(k) = k_w w_i(k)\} \quad (10)$$

$$X_i(k) \Leftarrow B_{i,m}(\alpha(k), \beta(k), \delta(k)) \otimes \begin{bmatrix} d_{i,m}(k) \\ w_{i,m}(k) \\ v_{i,m}(k) \end{bmatrix} \quad (11)$$

$$Y_i(k) \Leftarrow H_{i,n} \{(\gamma_0(k), \gamma_1(k), \dots, \gamma_n(k)) \otimes \begin{bmatrix} S(k) \\ S(k-1) \\ \dots \\ S(k-n) \end{bmatrix} \otimes G_i(k)\} \quad (12)$$

where

$$X \subset \bigcup_{z=1}^Z \overline{\text{supp}(z)} \quad (13)$$

$$\text{supp}(z) = \text{supp}(X_{z,1}) \times \text{supp}(X_{z,2}) \times \text{supp}(X_{z,3}) \quad (14)$$

$$Y_i = (Q_{i,h}, T_{i,h}, P_{i,h}) \quad (15)$$